

Phase integral of asteroids

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ABSTRACT

The values of the phase integral q were determined for asteroids using a numerical integration of the brightness phase functions over a wide phase-angle range and the relations between q and the G parameter of the HG function and q and the G_1, G_2 parameters of the HG_1G_2 function. The phase-integral values for asteroids of different geometric albedo range from 0.34 to 0.54 with an average value of 0.44. These values can be used for the determination of the Bond albedo of asteroids. Estimates for the phase-integral values using the G_1 and G_2 parameters are in very good agreement with the available observational data. We recommend using the HG_1G_2 function for the determination of the phase integral. Comparison of the phase integrals of asteroids and planetary satellites shows that asteroids have systematically lower values of q .

Key words. minor planets, asteroids: general – methods: numerical – techniques: photometric

1. Introduction

The phase integral q is one of the fundamental characteristics of light scattering by a planetary surface. It is related to the Bond albedo A ($A = pq$, where p is the geometric albedo; e.g., Shepard 2017). The Bond albedo is used in the thermal equilibrium equation to model thermal properties of asteroids (e.g., Morrison 1977; Tedesco et al. 2002; Delbó et al. 2003; Masiero et al. 2011; Usui et al. 2011). The phase integral has been defined as

$$q = 2 \int_0^\pi f(\alpha) \sin \alpha d\alpha, \quad (1)$$

where $f(\alpha)$ is the normalized disk-integrated phase function and α is the solar phase angle. A direct calculation of phase integrals is impossible for the asteroid majority owing to the limited phase-angle range of ground-based observations. Russell (1916) estimated the phase integral for the four asteroids (1) Ceres, (2) Pallas, (3) Juno, and (4) Vesta to be equal to 0.55 using an empirical law. We note that these are the largest objects of the asteroid belt. It is not completely clear whether any conclusions concerning these bodies can be simply generalized for the large number of smaller objects, which could have experienced different evolutions. Also according to Russell (1916), the phase integral can be derived from the value of the disk-integrated phase function at a phase angle of 50° .

Various researchers have used different estimates of the asteroid phase integral for analyzing data obtained in the infrared wavelength range. For example, Morrison (1977) deduced the value of the phase integral q to be equal to 0.6. In analyzing data

obtained from the Infrared Astronomical Satellite (IRAS), Wide-field Infrared Survey Explorer (WISE), and Akari satellites, a relationship between q and parameter G of the HG function (Bowell et al. 1989) was used (Tedesco et al. 2002; Masiero et al. 2011; Usui et al. 2011). Since for most asteroids the parameter G was considered to be equal to 0.15, this resulted in a value of the phase integral of 0.384 (Mainzer et al. 2011).

A rigorous determination of the phase integral needs measurements of the disk-integrated phase function over the range of phase angle from 0° to 180° . Unfortunately, ground-based observations allow observing of main-belt asteroids only from 0° to about 30° phase angles. In this range, the phase functions are well known for different asteroid taxonomical classes (e.g., Belskaya & Shevchenko 2000; Harris et al. 1989b; Shevchenko et al. 1997, 2008, 2012, 2015, 2016; Slivan et al. 2008; Slyusarev et al. 2012). Some data were obtained in a wider range of phase angles up to 90° for near-Earth asteroids (Harris et al. 1987; Kaasalainen et al. 2004; Mottola et al. 1997; Hicks et al. 2014, etc.), but such phase functions can be influenced by aspect variations (Muinonen & Wilkman 2016).

Space missions have allowed various phase functions to be determined up to 160° for different asteroids (Clark et al. 1999; Helfenstein et al. 1994; Masoumzadeh et al. 2015; Newburn et al. 2003; Spjuth et al. 2012, etc.), but the data at small phase angles are often not available. Space-based data complemented with Earth-based data acquired at small phase angles for some asteroids can be used for the numerical calculation of the phase integral. Such data were used by Helfenstein et al. (1994, 1996) for the determination of the phase integral of asteroids (951) Gaspra ($q = 0.47$) and (243) Ida ($q = 0.34$), by Clark et al. (1999)

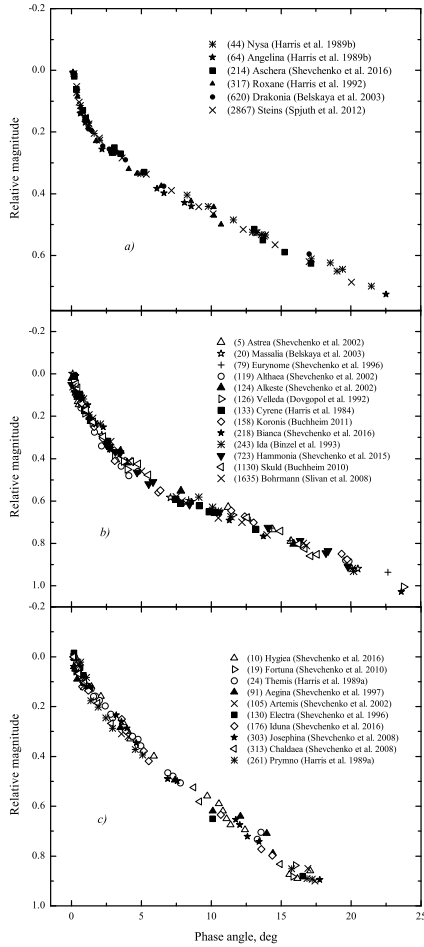


Fig. 1. Composite phase function of brightness at small phase angles for (a) high albedo ($p=0.39\text{--}0.53$), (b) moderate albedo ($p=0.15\text{--}0.25$), and (c) low-albedo ($p=0.045\text{--}0.10$) asteroids.

for (253) Mathilde ($q=0.28$), by Spjuth et al. (2012) for (2867) Steins ($q=0.59$), by Li et al. (2004) for (433) Eros ($q=0.40$), by Masoumzadeh et al. (2015) for (21) Lutetia ($q=0.40$), and by Tatsumi et al. (2018) for (25143) Itokawa ($q=0.13$). However, a detailed analysis of the phase integral for different asteroids, as has been carried out for planetary satellites (Verbiscer & Veverka 1988; Brucker et al. 2009), has not yet been performed. In this study, we investigate how the phase integral depends on the asteroid taxonomical class and compare the phase integrals of asteroids and planetary satellites.

2. Average phase functions of brightness in a wide range of phase angles

Detailed observations of the magnitude-phase dependencies of asteroids have revealed their similarity within the main taxonomical classes (Belskaya & Shevchenko 2000). We construct and present the composite magnitude-phase dependencies for high (E-complex), moderate (S-complex), and low albedo (C-complex) asteroids at small phase angles in Fig. 1.

These data were combined from observational data (Belskaya et al. 2003; Binzel et al. 1993; Buchheim 2010, 2011; Dvornikov et al. 1992; Harris et al. 1984, 1989a,b, 1992; Shevchenko et al. 1996, 2002, 2008, 2010, 2016; Slivan et al. 2008) of magnitude-phase dependencies of individual asteroids

(denoted by different symbols in the figures). Data alignment was applied using a shift along the magnitude axis to obtain the best fit between the curves. The alignment of phase curves was carried out by a minimum of the dispersion with linear least squares fit in the overlap region of $10\text{--}30$ degrees.

Although the low albedo asteroids show diversity in their brightness phase curves near the opposition, we used for these the average phase function at small α (Shevchenko & Belskaya 2010). The standard deviation of such a composite phase function is about 5%. To obtain the average phase functions of brightness for asteroids of high, moderate, and low albedo over a wide range of phase angles up to 160° , we used the most precise data from space observations (Clark et al. 1999; Masoumzadeh et al. 2015; Newburn et al. 2003; Spjuth et al. 2012). These data were supplemented with data from ground-based observations of some near Earth asteroids (Harris et al. 1987; Kaasalainen et al. 2004; Mottola et al. 1997). Such phase functions of brightness over a wide range of phase angles for selected asteroids are presented in Fig. 2. As is shown, the brightness behavior of asteroids with differing geometrical albedo shows differences mainly in the range of the opposition effect and in the range of phase angles of $120\text{--}140^\circ$.

These differences are small (not more than one magnitude) compared to the general brightness variations, but we took these differences into account and used the average phase function for high ($\sim 45\%$), moderate ($\sim 20\%$), and low albedo ($\sim 6\%$) asteroids to obtain a more reliable estimation of the phase integral.

3. Phase integrals for asteroids of different albedo

Figure 3 shows the functions $f(\alpha)\sin\alpha$ for moderate, high, and low albedo asteroids used to calculate the values of the phase integral for these groups. Since the value of the function $f(\alpha)\sin\alpha$ is zero at $\alpha=180^\circ$, this value was added for all asteroids for numerical calculation of the phase integral. It is also clear from the figure that the behavior of the functions $f(\alpha)\sin\alpha$ is similar in the range of phase angle from 0° to 10° , regardless of the albedo of the surface.

It should also be noted that the contribution of the values of the function $f(\alpha)\sin\alpha$ at phase angles $>115^\circ$ in the estimations of the phase integral does not exceed 1%. In addition, the maximum of the function $f(\alpha)\sin\alpha$ depends nonlinearly on the geometrical albedo of the asteroids. This requires an additional study because, unfortunately, data on the phase dependencies of brightness for asteroids with albedo $>60\%$ are absent. Moreover, the actual existence of asteroids having geometric albedo larger than 0.60 is uncertain. There are a few such objects in the asteroid belt, but their size is less than 15 km, which makes it difficult to obtain high-quality magnitude-phase relations for them.

By numerical integration of $f(\alpha)\sin\alpha$ for asteroids with different geometrical albedos, the values of their phase integrals are presented in Table 1. These values lie in the range from 0.35 to 0.54 with the average of 0.44.

The values of the phase integral can also be obtained by integrating the modeled phase functions. For example, the value of the phase integral of the well-known Lommel-Seeliger phase function is equal to 1.64 (e.g., Shepard 2017), which is much greater than that calculated from the measured phase functions. For real asteroid surfaces, shadowing among the regolith particles/structures causes a steep decrease of the phase curve and thus reduces the value of the phase integral. At present, several phase function models are used in planetary photometry with a number of free parameters for describing the properties

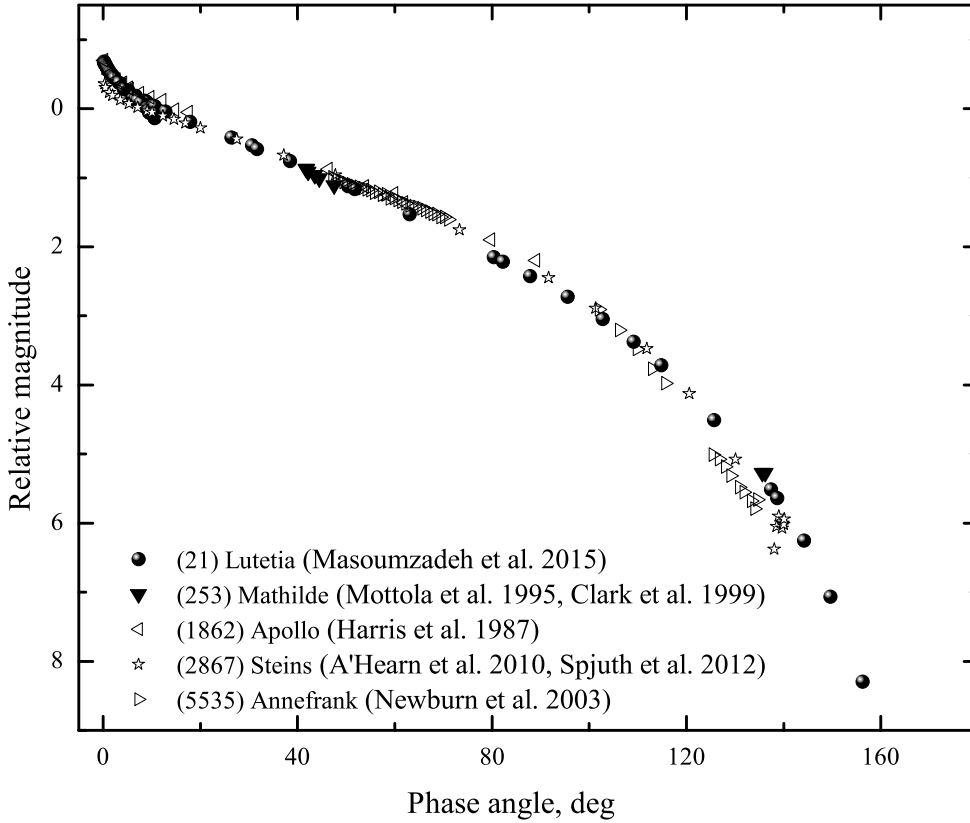


Fig. 2. Phase functions for selected asteroids over a wide range of phase angles: (21) Lutetia, S-complex, $p=0.19$ (Masoumzadeh et al. 2015); (253) Mathilde, C-complex, $p=0.047$ (Clark et al. 1999); (1862) Apollo, S-complex, $p=0.32$ (Nugent et al. 2015); (2867) Steins, E-complex, $p=0.39$ (A'Hearn et al. 2010; Spjuth et al. 2012); (5535) Annefrank, S-complex, $p=0.24$ (Newburn et al. 2003).

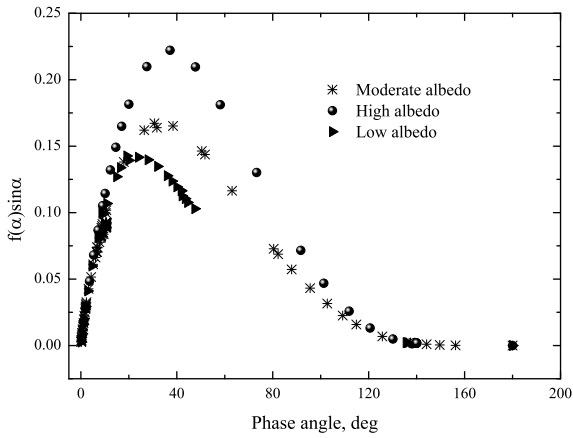


Fig. 3. Function $f(\alpha) \sin \alpha$ for high-, moderate-, and low-albedo asteroids.

of planetary surfaces (e.g., Hapke 2012; Bowell et al. 1989; Muinonen et al. 2010; Shkuratov et al. 2012, 2018). The often-used function by Hapke (2012) has a large number of parameters and requires both disk-integrated and disk-resolved data to retrieve these parameter values (Clark et al. 1999; Li et al. 2004; Simonelli et al. 1998; Thomas et al. 1996, etc.), but the results can still be ambiguous (Shkuratov et al. 2012). A new function proposed by Shkuratov et al. (2018) has a small number of parameters and works well for different classes of objects for both disk-integrated and disk-resolved data. But currently these parameters have not been estimated for asteroids of different albedos and the connection between the phase integral and these parameters has not been studied. We used the HG and HG_1G_2 functions (Bowell et al. 1989; Muinonen et al. 2010), which were recommended by the International Astronomical Union as

magnitude systems in asteroid integral photometry. There are relationships of the phase integral with parameter G (Bowell et al. 1989), i.e.,

$$q = 0.290 + 0.684G, \quad (2)$$

and G_1 and G_2 (Muinonen et al. 2010), where

$$q = 0.009082 + 0.4061G_1 + 0.8092G_2, \quad (3)$$

for these functions. Typical dispersion of the G parameter among asteroids is 0.10, and 0.05 for G_1 and G_2 . Using the average parameters of G , G_1 , and G_2 for the main taxonomical classes (Shevchenko & Lupishko 1998; Shevchenko et al. 2003, 2016) and the relations between q and these parameters, the average values of the phase integral for asteroids with different albedo surfaces were obtained. These data are listed in Table 1 where the values of the phase integral calculated with formulas (1)–(3) are presented.

The average values of the phase integral calculated from the observations and from the HG and HG_1G_2 functions coincide well, although the value of the phase integral for high albedo asteroids using the HG model has a significantly greater value. However, it should be noted that the HG function has a reduced brightness in the area of the opposition region relative to real behavior, in contrast to the HG_1G_2 function, which more accurately approximates the phase dependency of brightness. Thus, the HG_1G_2 function produces results that are more accurate when brightness values are only available in the range of phase angles from 0° to 30° .

The values of phase integral for moderate albedo asteroids are close to the values obtained by Helfenstein et al. (1994) for the asteroid (951) Gaspra ($q=0.47$), by Li et al. (2004) for (433) Eros (0.40), by Masoumzadeh et al. (2015) for (21) Lutetia (0.40), and by Hicks et al. (2014) for (4) Vesta (0.44), although

Table 1. Values of the phase integral for asteroids of differing geometrical albedo.

Complex	Geometrical albedo	Observations	Phase integral q	
			HG function	HG_1G_2 function
Low albedo	0.061 ± 0.017	0.35 ± 0.02	0.34 ± 0.03	0.36 ± 0.02
Moderate albedo	0.20 ± 0.05	0.42 ± 0.02	0.45 ± 0.02	0.42 ± 0.02
High albedo	0.45 ± 0.07	0.54 ± 0.02	0.63 ± 0.04	0.56 ± 0.03
Average	0.24 ± 0.20	0.44 ± 0.10	0.47 ± 0.15	0.45 ± 0.10

Notes. The phase integral q for the observations was computed with numerical integration. The error bars are the 1 sigma dispersion in the calculated values.

this asteroid has an albedo of about 40%. The values of the phase integral for low albedo asteroids obtained in this work differ significantly from the values obtained by [Clark et al. \(1999\)](#) for the low albedo asteroid (253) Mathilde ($q=0.28$). In our opinion, this is due to the inadequate combination of phase dependencies derived from Earth-based observations ([Mottola et al. 1995](#)) and spacecraft data for this asteroid. We also obtained the value of the phase integral for (1) Ceres using data for phase function of brightness from [Ciarniello et al. \(2017\)](#) and [Tedesco et al. \(1983\)](#). The value is equal to 0.35 ± 0.02 and is typical for low albedo asteroids.

4. Comparison with planetary satellites

Using the values of the parameters G_1 and G_2 ([Shevchenko et al. 2016](#); [Penttilä et al. 2016](#)) for about 100 different-type asteroids, the values of the phase integral were determined and compared with those obtained by [Brucker et al. \(2009\)](#) for planetary satellites. In addition, the phase dependencies of brightness for the Moon, Phobos, and Deimos ([Avanesov et al. 1991](#); [Bowell et al. 1989](#); [Rougier 1933](#); [Velikodsky et al. 2011](#)) were used for the determination of their phase integrals, which are 0.48 ± 0.02 , 0.38 ± 0.03 , and 0.40 ± 0.03 , respectively. Our value of the phase integral for Phobos (0.38 ± 0.03) differs from the value of 0.30 ± 0.04 obtained by [Simonelli et al. \(1998\)](#), although the value for Deimos (0.40 ± 0.03) is in agreement with the value of 0.39 ± 0.02 obtained by [Thomas et al. \(1996\)](#). In the case of the Moon, our value is very different from the value 0.60 obtained by [Lane & Irvine \(1973\)](#). We assume that it is related to the use of new, better quality data on the phase function of the Moon obtained by [Velikodsky et al. \(2011\)](#). Figure 4 shows the dependency of the phase integrals for asteroids and planetary satellites as a function of their geometrical albedos. It should be noted that the albedo range is wider for the satellites and there are currently no data on the phase integrals for asteroids with albedos greater than 60%.

In Fig. 4, the solid line shows a linear fit for the satellites without Phoebe and Europa, and a dot-dashed line shows a linear fit when Phoebe and Europa are included. We added data for the Moon, Phobos, Deimos, and asteroids on the satellite diagram without a recalculation of the linear fits for the satellites given by [Brucker et al. \(2009\)](#). The dashed line shows a linear fit only for the asteroids ($q=0.359 (\pm 0.005) + 0.47 (\pm 0.03) p$). In general, the values of phase integrals of satellites are systematically larger than for asteroids. This indicates that the linear part of phase functions of the asteroids has a greater slope than for the satellites. This result remains to be interpreted from a theoretical point of view. An exception is the Saturnian satellite Phoebe that has the lowest value of the phase integral among the objects

under study. The Martian satellites Deimos and Phobos, and the Uranian satellite Miranda have phase-integral values similar to those of asteroids. When extrapolating the asteroid phase integrals to albedos greater than 60%, we retrieved values similar to those of the Saturnian satellites of Rhea, Tethys, and Enceladus, i.e., not greater than 0.8. If this extrapolation holds true, then we can expect that for such asteroids, the phase function differs from the behavior of E-type asteroids and their thermal properties may not correspond to the developed thermal models for high-albedo asteroids.

5. Conclusions

Based on the results of ground-based observations and data obtained from space missions, the composite average phase dependencies of brightness for moderate, high, and low albedo asteroids in a wide range of phase angles from 0° to 160° were obtained. Because the phase functions of brightness for asteroids inside a taxonomical class behave similarly, it is possible to estimate the value of the phase integral for that asteroid class using a representative phase function.

The values of the phase integral q were determined for asteroids of different albedos using both a numerical integration of the average brightness phase functions over a wide phase-angle range and the relations between q and the G parameter of the HG function and between q and the G_1 , G_2 parameters of the HG_1G_2 function. The values of the phase integral lie in the range from 0.34 to 0.63 with an average of 0.45. These data can be used to model the thermal properties of asteroid surfaces and to process data obtained in the infrared wavelength range.

The behavior of the function $f(\alpha) \sin \alpha$ is similar in the range of phase angle from 0° to 10° , regardless of the surface albedo. Moreover the contribution of the function $f(\alpha) \sin \alpha$ at phase angles greater than 115° using an estimation of the phase function does not exceed one percent, and has a limited impact on the value of the phase integral calculated. In addition, the maximum of the function $f(\alpha) \sin \alpha$ depends nonlinearly on the asteroid albedo. Such behavior warrants additional study, but, unfortunately, data on phase dependencies of brightness for asteroids with albedos greater than 60% are absent. An estimation of the phase-integral values using G_1 and G_2 parameters gives a very good agreement with data obtained from space missions. We recommend using the HG_1G_2 function for the determination of the phase integral. In the case of an unknown phase function for an asteroid, it makes sense to use the average value of the phase integral for an asteroid of corresponding albedo and/or the linear dependency on albedo. The differences in the values of the phase integral for asteroids of different classes are important to take into account in thermal modeling.

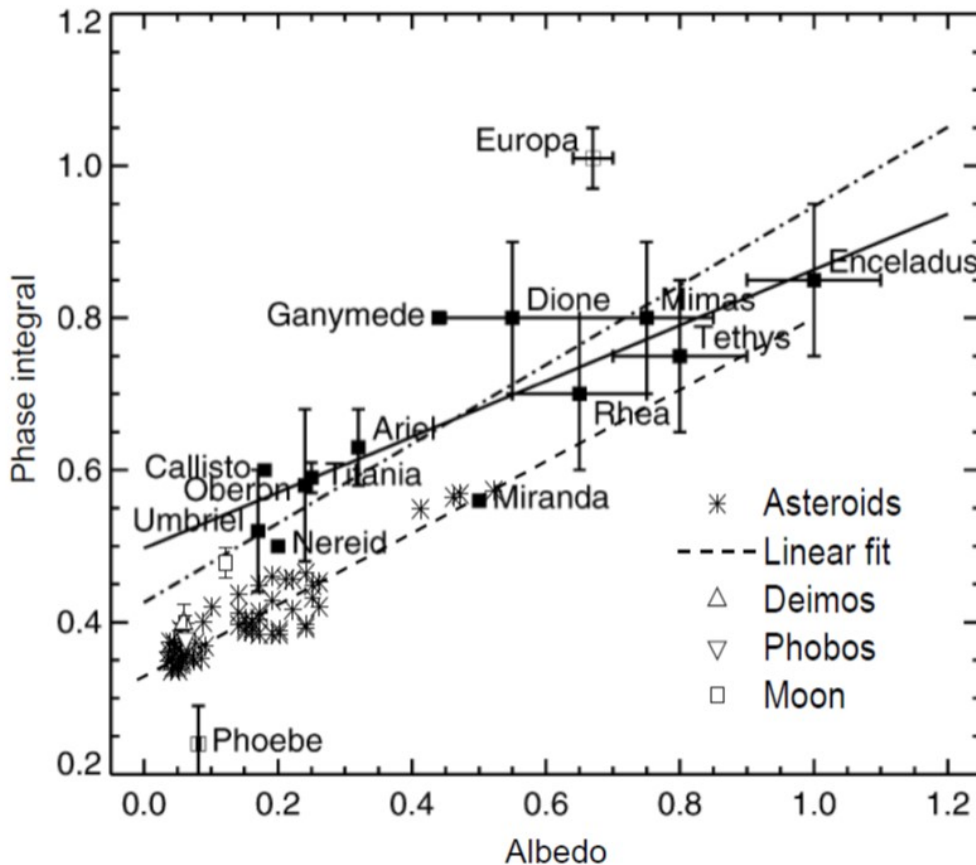


Fig. 4. Dependency of the phase integral on the geometric albedo for asteroids and planetary satellites. The dashed line is the best linear fit to the asteroid data. The solid line is the adopted best linear fit to the satellite data without including Phoebe and Europa and the dot-dashed line is the best linear fit to the data including Phoebe and Europa. The satellite data are adapted from Brucker et al. (2009).

A comparison of the phase integrals shows that asteroids have systematically lower values than planetary satellites having the same albedo. Moreover, when asteroid phase integrals are extrapolated into regions of greater albedo, their values are less than 0.8. As mentioned above the actual existence of asteroids having geometric albedo larger than 0.60 is uncertain. It can be expected that, for asteroids, the phase integral cannot exceed the value of 0.8.

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